

Filling-Dependent Intertwined Electronic and Atomic Orders in the Flat-Band State of 1T-TaS₂

Yanyan Geng,[#] Haoyu Dong,[#] Renhong Wang,[#] Jianfeng Guo, Shuo Mi, Le Lei, Yan Li, Li Huang, Fei Pang, Rui Xu, Weiqiang Yu, Hong-Jun Gao, Wei Ji,^{*} Weichang Zhou,^{*} and Zhihai Cheng^{*}



Cite This: <https://doi.org/10.1021/acsnano.4c13437>



Read Online

ACCESS |



Metrics & More



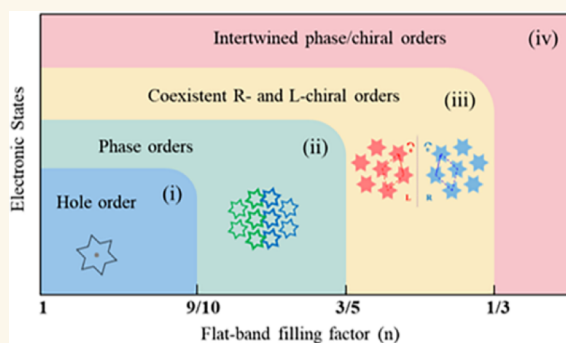
Article Recommendations



Supporting Information

ABSTRACT: The delicate interplay among the complex intra/inter-layer electron–electron and electron–lattice interactions is the fundamental prerequisite of these exotic quantum states, such as superconductivity, nematic order, and checkerboard charge order. Here, we explore the filling-dependent multiple stable intertwined electronic and atomic orders of the flat-band state of 1T-TaS₂, encompassing hole order, phase orders, coexisting left- and right-chiral orders, and mixed phase/chiral orders via scanning tunneling microscopy (STM). Combining first-principles calculations, the emergent electronic/atomic orders can be attributed to the weakening of electron–electron correlations and stacking-dependent interlayer interactions. Moreover, achiral intermediate ring-like clusters and nematic charge density wave (CDW) states are successfully realized in intralayer chiral domain wall and interlayer heterochiral stacking regions through chiral overlap configurations. Our study not only deepens the understanding of filling-dependent electronic/atomic orders in flat-band systems but also offers perspectives for exploring exotic quantum states in correlated electronic systems.

KEYWORDS: charge density wave, flat-band, electron–electron correlations, interlayer interaction, scanning tunneling microscopy, electronic and atomic orders



The transition metal dichalcogenides (TMDs) deserve particular attention as they exhibit rich electronic states, such as charge density wave (CDW),^{1–3} superconductivity (SC),^{4,5} quantum spin liquid,⁶ magnetism,⁷ etc. Most of these electronic states depend on the competition, coexistence, or cooperation of electron–electron correlations and electron–lattice interactions and, therefore, are significantly sensitive to variations in the electronic structures.^{8,9} Hole or electron doping has been an effective way to tune the electronic structures. For example, CDW is very rapidly suppressed in hole Sn-doped CsV₃Sb₅,¹⁰ superconductivity occurs in electron/hole-doped twisted graphene moiré superlattice systems,^{11,12} and superconductivity is enhanced in electron K-doped FeSe.¹³ Meanwhile, precise carrier doping can also gradually modulate the internal electron–electron correlation, leading to the induction of intriguing quantum states, including checkerboard charge order,^{14,15} nematic phase,¹⁶ a superconducting dome,¹⁷ a correlation-driven insulating phase,^{18,19} and a metallic phase.^{20,21} Therefore, a detailed study of the structure and properties of the doping-related electrons is a

necessary prerequisite for achieving controllability of CDW-based exotic quantum states.

Among various TMD materials, 1T-TaS₂ has attracted wide attention due to its abundant CDW phase.^{22–24} The formation of the Star of David (SoD) in the CDW state creates a half-filled flat band, which is transformed into a Mott insulator or band insulator by electronic correlations or interlayer coupling.^{25–27} Meanwhile, because of the close proximity of the various competing interactions in energy, doped electron or hole carriers can modify the flat-band filling factor and effectively modulate the electron correlation effects in CDW to achieve a rich variety of quantum states.^{28–30} Prominent examples include metallization, which can be realized without

Received: September 24, 2024

Revised: February 8, 2025

Accepted: February 10, 2025

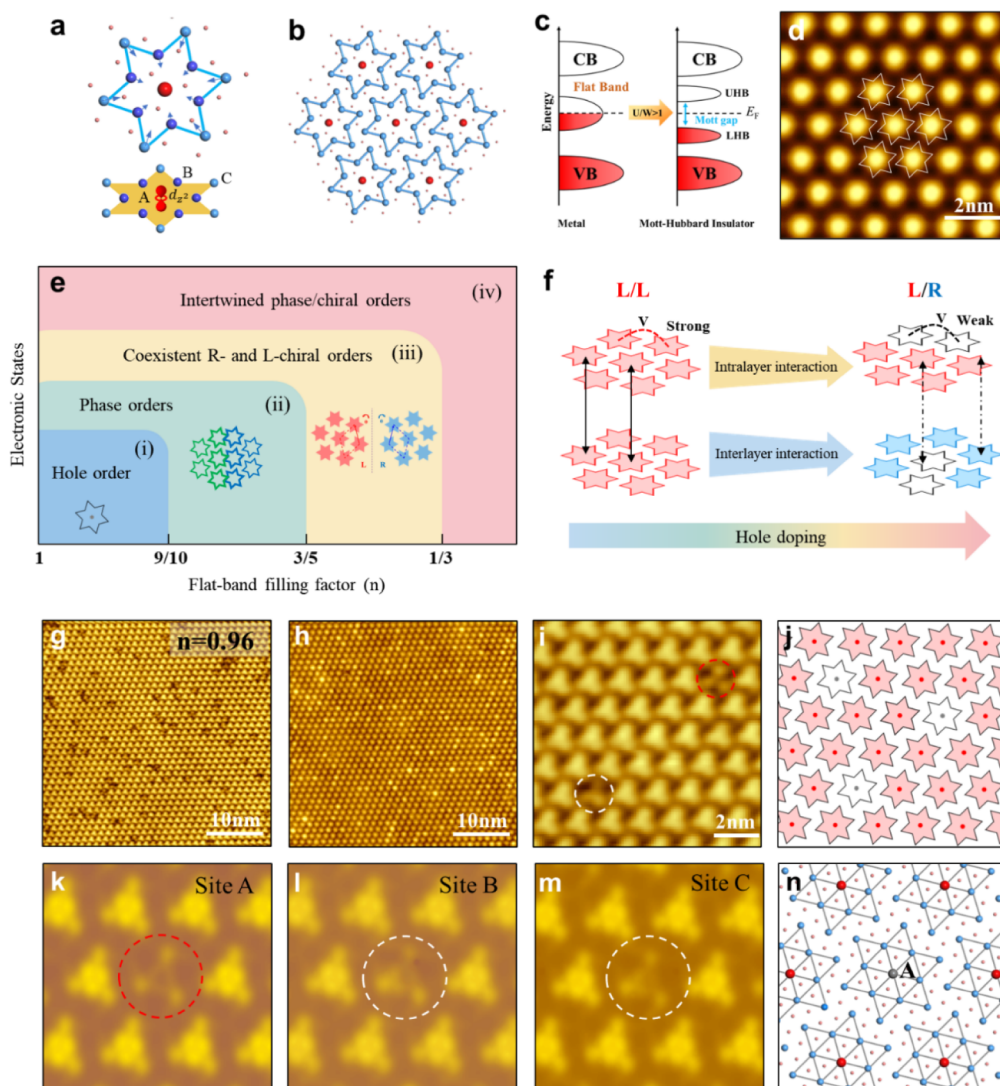


Figure 1. Structure model of filling-dependent intertwined electronic and atomic orders of $1T\text{-TaS}_2$. (a) Atomic models of the SoD cluster with the localized d_{z^2} orbital (unpaired electron) of the central Ta atom. (b) Schematic of the SoD clusters with the $\sqrt{13} \times \sqrt{13}$ periodicity. (c) Schematic band structures of the correlated CDW state, in which the half-filled flat band of the localized d_{z^2} orbital is split into UHB and LHB bands via electron correlations. (d) STM image of the commensurate CDW state with the overlaid SoD models. (e) Schematic diagram of electronic orders and flat-band filling factors of $1T\text{-TaS}_2$. Each SoD is fully centrally electron-filled, corresponding to a flat-band filling factor $n = 1$ for $1T\text{-TaS}_2$. While each SoD is fully central electron-empty, corresponding to a flat-band filling factor $n = 0$ for $1T\text{-TaS}_2$. (f) Schematic of the delicate interplay of the complex intralayer and interlayer interactions with hole doping. (g–i) Large-scale occupied state (g), unoccupied state (h), high-resolution (i) STM images of hole order at the flat-band filling factor $n = \sim 0.96$. (j) Structure model of electron-filled and -empty SoDs. The central electron-filled and -empty SoDs are marked by the central red and gray dots, respectively. (k–m) Simulated STM images of the three inequivalent substitution sites: site A (k), site B (l), and site C (m). (n) Structure model of the inequivalent substitution site A. Scanning parameters: (g,i) $V = -0.4$ V, $I = -100$ pA; (h) $V = 0.4$ V, $I = 100$ pA.

breaking the long-range CDW order when surface electron doping is applied,^{27,31} while hole doping is known to drastically suppress the transition from a nearly commensurate CDW (NCCDW) phase to a commensurate CDW (CCDW) phase,³² and superconductivity coexists with CDW.³³ Furthermore, doping not only can directly affect the interior electron–electron correlations but also induce significant changes in the interlayer CDW stacking order.²² Despite extensive previous studies on doping, it is still important to understand the evolution of filling-dependent electronic and atomic orders in the flat-band state based on intralayer and interlayer interactions.

In this work, we investigate the filling-dependent intertwined electronic and atomic orders in the flat-band state and internal

interlayer/intralayer interactions of $1T\text{-TaS}_2$ by STM combined with theoretical calculations. With decreasing flat-band filling factor, a variety of interleaving orders are observed: hole order, phase orders, stacking disorder, and intertwined phase/chiral orders in sequence. The emergence of a stable fragmented intralayer phase domain can be attributed to the reduced electron–electron correlations, which are incapable of persisting long-range intralayer orders. The further decreased electron–electron correlations and interlayer interactions contributed to the following appearance of intralayer chiral domains and interlayer heterochiral stacking. At the intralayer chiral domain wall and interlayer heterochiral stacking regions, the intermediate ring-SoD clusters and nematic CDW states are discovered and discussed based on

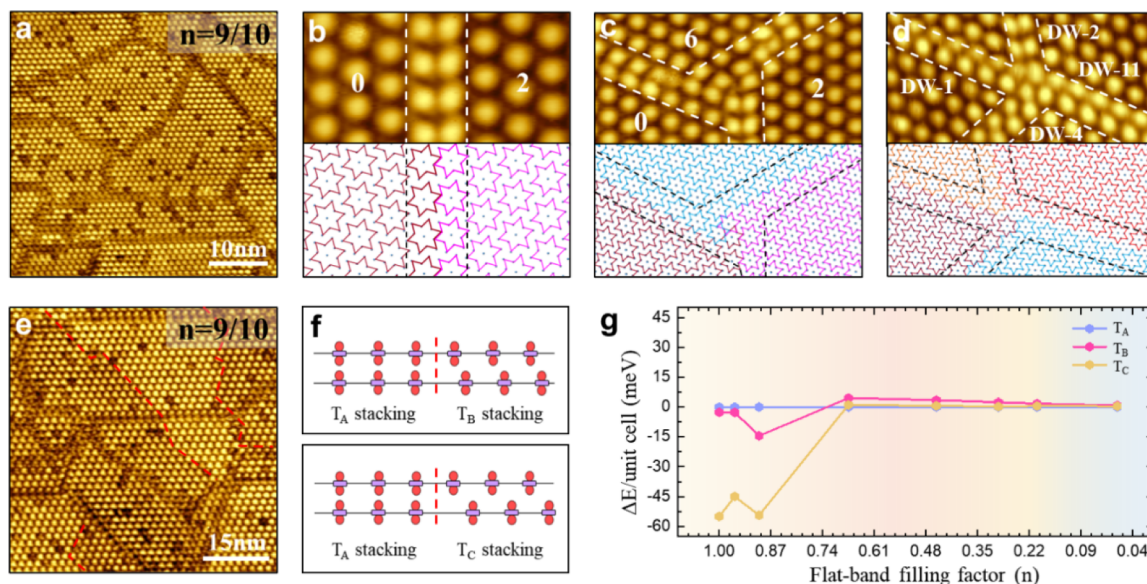


Figure 2. Emergence of phase domains at the flat-band filling factor $n \approx 9/10$ of $1T\text{-TaS}_2$. (a) Large-scale STM images of the emergent phase domains of $1T\text{-TaS}_2$. (b) STM images of typical CDW phase DWs (top) and their schematic structural configurations (bottom). The constituent SoDs of phase DWs are highlighted by the dashed lines separating the two neighboring phase domains. (c,d) STM images of two typical CDW vortices and their schematic structural configurations. (e) STM images for sublayer phase DWs. The red lines denote the phase DWs of the sublayer. (f) Arrangement of the localized states of the central Ta atoms for the three representative CDW stacking configurations: T_A , T_B , and T_C . (g) First-principles calculations of the T_A , T_B , and T_C stacking configurations as a function of the flat-band filling factor in $1T\text{-TaS}_2$. Scanning parameters: (a,e) $V = -0.4$ V, $I = -100$ pA; (b–d) $V = 0.4$ V, $I = 100$ pA.

the transient chiral-overlapping interactions. This work provides important insights into internal interactions and the future realization of exotic quantum states in correlated electronic materials.

RESULTS AND DISCUSSION

The ground CDW state of $1T\text{-TaS}_2$ is characterized by the commensurate $\sqrt{13} \times \sqrt{13}$ superlattice of SoD clusters, as depicted in Figure 1a,b. The SoD cluster is made of 12 inward-distorted outer Ta atoms and one center Ta atom, in which the 12 Sd_{z^2} electrons of the outer Ta atoms pair and form six occupied CDW valence bands. The remaining one unpaired electron of SoD is maximally localized at the central Ta atom to form the half-filled flat band. A relatively strong intralayer electron–electron correlation then leads to the split upper Hubbard band (UHB) and lower Hubbard band (LHB), forming a correlated Mott insulator without considering the interlayer interaction (Figure 1c). Recently, the important role of the interlayer stacking order has been emphasized, and the ground CCDW state of $1T\text{-TaS}_2$ can be described as a trivial band insulator/conventional Mott insulator on the termination of T_A/T_C stacking at low temperatures.^{25–27} Figure 1d presents the STM image of the ground CCDW state with the overlaid star models of the SoDs.

Hole doping can effectively modify the flat-band filling factor, providing an exemplary platform to fine-tune the electronic/atomic structure and realize a wide range of intriguing electronic states. Figure 1e illustrates the schematic diagram of electronic orders and flat-band filling factors, which shows the evolution of a series of electronic orders: (i) hole order, (ii) phase orders, (iii) coexisting left- and right-chiral orders, and (iv) intertwined phase/chiral orders. Notably, the phase and chiral domains created by hole doping can reach the millimeter scale in a stable state, in contrast to the various metastable domains induced by pressure, ultrafast optical, and

electrical pulses.^{34–38} These emergent electronic states can be phenomenologically attributed to the competition and cooperation of stacking-dependent interlayer interactions and intralayer interactions of $1T\text{-TaS}_2$ (Figure 1f). In $1T\text{-TaS}_2$, with the increase of hole doping, the reduction of intralayer electrons contributes to the gradual weakening of electron–electron correlation, resulting in the inability of the CCDW to maintain long-range ordering and the emergence of hole and phase/chiral domain walls (DWs). Meanwhile, hole doping is also accompanied by the gradual diminishing of interlayer SoD interactions (T) (Figure S1),²² which leads to the emergence of random stacking order and interlayer heterochiral stacking.

Compared to the pristine $1T\text{-TaS}_2$, the slight reduction of flat-band filling electrons results in the appearance of hole-SoDs within the CCDW superlattice, showing darker (brighter) contrast than the normal SoDs at the occupied (unoccupied) state, as shown in Figure 1g,h. These hole-SoDs are clearly resolved as the darker three-petal flower shapes in the high-resolution STM image of Figure 1i and are further schematically illustrated in Figure 1j. To determine the origin of the three-petal flower SoD, first-principles calculations and dI/dV spectra are performed. It can be seen that the typical dI/dV spectra of bright triangular SoDs and dark three-petal flower SoDs show significant differences (Figure S2). The bright SoDs display an electron–hole symmetric gap, while the dark SoDs exhibit an electron–hole asymmetric single pronounced peak that onsets sharply above the Fermi energy. According to the first-principles simulation, the three-petal flower SoDs can be well reproduced by selecting the central (site A) or peripheral Ta (site B or C) as the Ti substitution sites, as shown in Figures 1k–n and S3. Since the central (site A) has the lowest doping energy (Table S1), we suggest that the three-petal flower SoDs originate from the substitution of Ti atoms for the central Ta atoms, leaving the SoDs without central Mott electrons.

The obvious effect of the reduction of the flat-band filling factor is to create domains of diverse shapes and sizes separated by sharp DWs (Figure 2a). Most DWs are formed straight along the CCDW unit vector with a single-phase shift between two adjacent CCDW domains, as shown in Figures 2b, S4, and S5. In addition, the DWs also construct complex DW junctions, including X, Y, and so on (Figure 2c,d). It is worth noting that the mosaic-like CDW states are the stable ground state in thermal equilibrium, which is existent in each layer and different from the metastable (by the external energy excitations) mosaic state of surface layers in pristine 1T-TaS₂ in recent reports (Figure S6).³⁶

Interestingly, in addition to the DWs in the surface layer, there are extra but weaker domain walls within a relatively large single domain (indicated by the red dashed lines in Figure 2e), which are assigned as the sublayer DWs.^{36,41} These subdomains correspond to different interlayer CDW stacking configurations (Figure 2f), resulting in different apparent contrasts in the surface-sensitive STM images. The calculation results (Figures 2g and S7) show that the flat-band filling factor has a dramatic effect on the stability of interlayer CDW stacking configurations. In the case of a flat-band filling factor of $n = 1$, T_C stacking dominates. As the filling factor decreases, the energy of T_C stacking gradually increases (Table S2). At the flat-band filling factor $n = \sim 3/5$, the energies of the various stacking configurations are similar, and the stacking order is random. This means that doping reduces the stacking-dependent interlayer interactions, leading to various local interlayer stacking configurations, which increases the complexity of these mosaic-like CDW states.

In 1T-TaS₂, SoD can also be arranged into different chiral domains: *L*-chiral and *R*-chiral, as shown schematically in Figure 3a,b. The SoD superlattices are rotated clockwise from the Ta atomic lattice by -13.9° and $+13.9^\circ$ in the *L*- and *R*-chiral-arranged CDW domains, respectively. In general, the lateral size of the $\sqrt{13} \times \sqrt{13}$ domain of a SoD superlattice in 1T-TaS₂ is much larger than the normal scan range of STM measurements of about a few hundred nanometers,³⁹ and their interlayer stackings are almost exclusively preferred to the homochiral stacking even in different phase stacking configurations. Only very few works about the chiral CDW state were reported recently, with the focus on their global chiral-switching via circularly polarized light or electrical pulse in the nanothick flakes.^{40,41}

At the flat-band filling factor $n = \sim 3/5$, large chiral CDW domains emerge within the mosaic-like CDW states, as shown by the marked chiral DWs that separate the *R*- and *L*-chiral domains in Figure 3c,d and the corresponding FFT pattern. The large chiral domains are made of many small homochiral phase domains, as schematically illustrated in Figure 3e. It is also noted that, different from the DWs at the low-doping level, the DWs could not be readily resolved based on their specific local contrast. At the flat-band filling factor $n = \sim 1/3$, the fragmentized CDW states are observed, made of randomly distributed tiny phase and chiral domains, as shown in Figure 3f,h. The short phase and chiral DWs are disordered and could not be clearly defined. The atomic- and SoD-resolution characterizations of these fragmented DWs were further performed, as depicted in Figure 3g, indicating the perfect continuous atomic lattice across the DWs without any visible doping-induced atomic defects and/or dislocations.

The mirror-symmetric chiral DWs along the [110] and [211] directions of the atomic lattice are illustrated in Figures

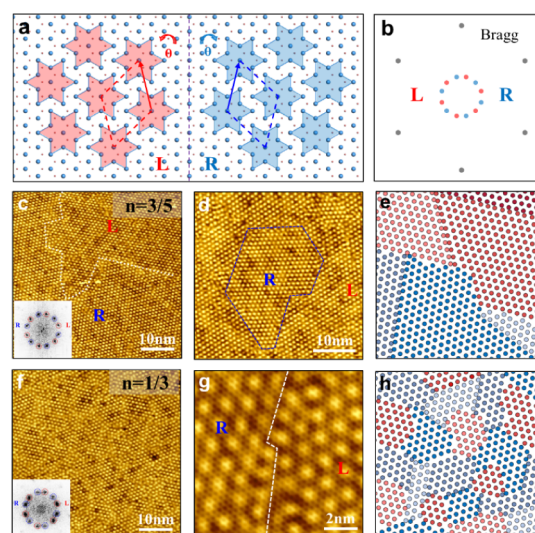


Figure 3. Filling-dependent intertwined phase and chiral orders of 1T-TaS₂. (a) Schematic of *L*- and *R*-chiral CDW domains. The unit cells of *L*- and *R*-chiral domains are shaded in red and blue, respectively. (b) Schematic FFT pattern of *L*- and *R*-chiral CDW domains with the atomic Bragg spots. (c,d) Large-scale STM images of the emergent chiral domain wall at the flat-band filling factor $n = 3/5$ of 1T-TaS₂. The chiral DW is along the [110] direction of the *R*-chiral domain and marked by blue dashed lines in (d). (e) Structural model of chiral domains. The emergent large chiral-arranged CDW domain is made of many small homochiral phase domains. (f) Large-scale STM images of intertwined chiral and phase domains at the flat-band filling factor $n = \sim 1/3$ of 1T-TaS₂. (g) Atomic-resolution STM image of typical chiral DWs. The chiral DW is marked by white dashed lines. (h) Structural model of mixed chiral/phase domains. The fragmentized CDW state is made of a randomly distributed tiny phase and chiral domains. Scanning parameter: $V = 0.4$ V, $I = 100$ pA.

4a and S9. The chiral DWs along the [110] direction are mostly observed in STM images, as shown in Figure S10, which should be relatively stable considering the complex inter-SoD interactions around the chiral DWs. Particularly, such chiral DWs easily form the intermediate ring-SoD clusters with a unique central achiral SoD as an anchor point, as indicated by the black dashed circles in Figure 4b. By variable-temperature STM, the STM image containing the ring-SoD cluster features is successfully attained at 50 K (Figure 4c). In contrast to single chiral domains, such ring-SoD clusters are rarely observed and are found only in larger chiral domains with a flat-band filling factor $n = \sim 3/5$. The ring-SoD clusters (white dashed circles) typically have a lateral size of $\sim 5 \times 5$ nm and are surrounded by chiral DWs. Interestingly, these ring-SoD clusters act as thermally excited dynamic structures that can move along the chiral DW and act as intermediate electronic states of the SoD during chiral transitions (Figure S11). The evolution of chiral transitions via intermediate ring-SoD clusters is further visualized in Figure 4d, which is schematically illustrated by the atomic model in Figures 4e and S12.

Next, we concentrate on the evolution of the metastable intermediate ring-SoD clusters. The sequential *in situ* STM characterizations (identified by the bright spots) provide a detailed insight into the dynamics of the chiral changes in CDW superlattices (Figure 4f–i). It can be seen that the two chiral domains change over time, with the *R*-chiral domain

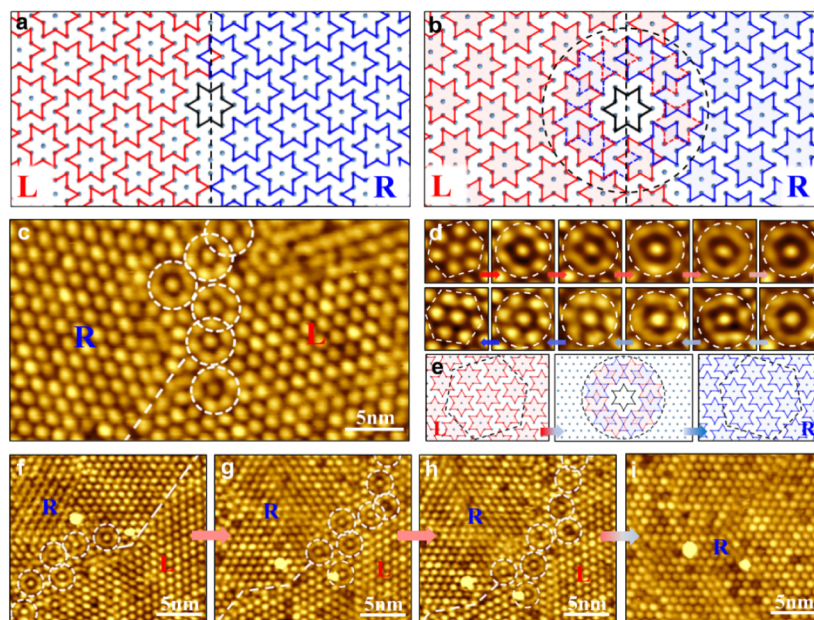


Figure 4. Emergence of intralayer ring-SoD clusters on the chiral domain wall of 1T-TaS₂. (a) Atomic structural model of the chiral DW along the [110] direction. This kind of chiral DW is mostly observed in STM images, which should be relatively stable considering the complex intra-SoD interactions around the chiral domain walls. (b) Chiral-SoD-overlapping model of the mirror-symmetric DW with the central achiral SoD (black star). (c) STM images of the emergent intermediate ring-SoD clusters around the chiral DWs of 1T-TaS₂. (d,e) High-resolution STM images and structural models of a series of dynamic intermediate ring-SoD cluster configurations from *L*-chiral SoD to *R*-chiral SoD, phenomenally indicating the structural evolution of SoDs and the process of chiral-switching transition. (f–i) Sequential *in situ* STM images showing dynamic chiral-switching of ring-SoD clusters at the chiral DWs. The ring-SoD clusters are marked with the dashed circles. Scanning parameters: $V = 0.4$ V, $I = 100$ pA.

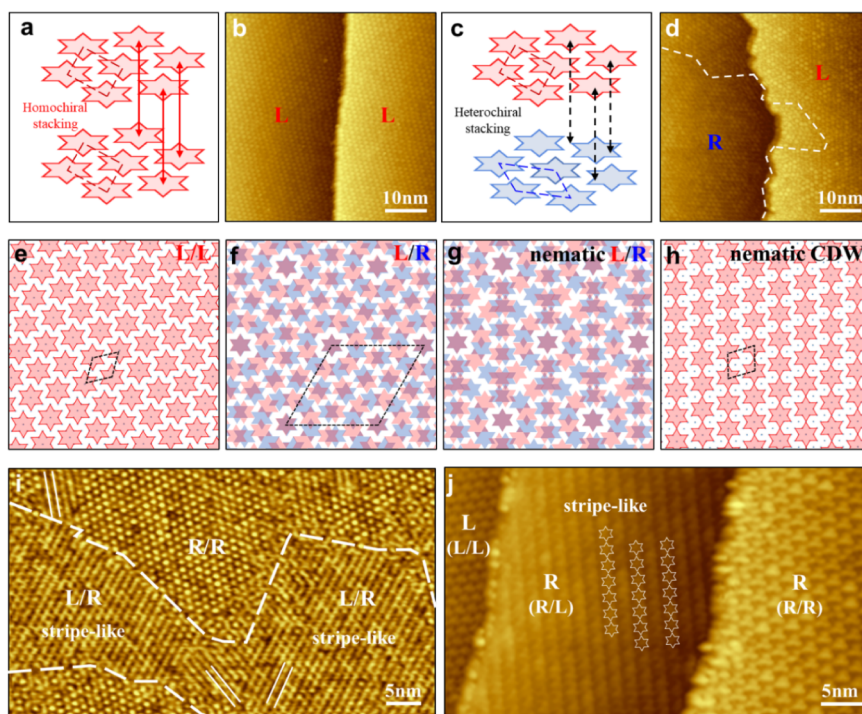


Figure 5. Interlayer heterochiral CDW stacking and the emergent nematic CDW state of 1T-TaS₂. (a,b) Schematics and STM images of the step edge in homochiral CDW stacking configurations. (c,d) Schematics and STM images of the step edge in heterochiral CDW stacking configurations. (e,f) Illustration of CDW superstructures for homochiral *L/L* and heterochiral *L/R* stacking. Unit cells of the CDW superstructures are outlined in black. (g) Proposed directional relaxed heterochiral stacking configurations for the observed stripe-like pattern of nematic *L/R* stacking. (h) Structural model of the stripe-like nematic CDW state. (i) Large-scale STM image of the chiral domain with the emergent stripe-like nematic CDW state due to the heterochiral stacking configuration. (j) STM image of two step edges with respective homochiral/heterochiral stacking configurations and the accompanying stripe-like feature of nematic CDW state. Scanning parameters: (b,d,j) $V = -0.4$ V, $I = -100$ pA; (i) $V = 0.4$ V, $I = 100$ pA.

expanding and the L -chiral domain gradually shrinking, until it eventually all transforms into a structural domain with a single R chirality (Figure 4i). Moreover, the atomic arrangement of the CDW superlattice remains continuous and intact after the change of chirality. In $1T$ -TaS₂, electron–electron correlation and e – ph interaction are key factors in the formation of a SoD cluster. As the flat-band filling factor decreases, the number of correlated electrons reduces, leading to a weakening of electron–electron correlation. Meanwhile, the ring-SoD clusters serve as the intermediate states during chiral transitions, causing the redistribution of atoms and the renormalization of the phonon frequency. Therefore, we suggest that the appearance of the ring-SoD structure can be phenomenologically attributed to the electron–electron correlation and e – ph coupling.

In $1T$ -TaS₂, the manipulation of interlayer stacking allows for the construction of customizable quantum systems exhibiting exotic physics. The models of the homochiral and heterochiral CDW units are depicted in Figure 5a,c. The STM experiments can easily identify the CDW chirality of both layers by measuring the angle between the close-packed direction of SoD and the step edges, which directly visualizes the two different stacking structures of homochiral L/L and heterochiral L/R CDW stacking orders, as shown in Figure 5b,d. At near full filling of the flat band, no obvious chiral domains are observed in both the upper and lower layers, showing homochiral stacking (Figure 5b), which is consistent with pristine $1T$ -TaS₂.^{42–45} At half-filling of the flat band, the reduction of electron–electron correlation contributes to the appearance of chiral domains; meanwhile, the weakening of interlayer interactions is accompanied by the simultaneous emergence of two different chiral domains in both the upper and the lower layers, resulting in heterochiral stacking (Figure 5d).

In contrast to the homochiral L/L stacking configuration (Figure 5e), a 27.8° rotational mismatch between the L - and R -layer CDWs in the heterochiral L/R stacking configuration contributes to a commensurate CDW moiré superstructure (Figure 5f). In the CDW moiré unit cell (black diamond-shaped box in Figure 5f), the relaxed atomic structure transforms from a ($\sqrt{13} \times \sqrt{13}$) R13.9° triangular superlattice to a larger 13×13 supersuperlattice. This superstructured CDW state is energetically very unfavorable and susceptible to spontaneous symmetry breaking, inducing a redistribution of atoms into a nematic structure. We propose the possible formation of the intermediate nematic L/R structure (Figure 5g) and the final nematic CDW configuration after structural relaxation of the superstructure generated by CDW chiral coexistence (Figure 5h).

Real-space investigations of the nematic CDW state at heterochiral L/R stacking interfaces are presented in Figures Si and S13. By statistically analyzing the areas occupied by homochiral L/L (R/R) stacking structures and the areas occupied by heterochiral L/R (R/L) stacking configurations, we can roughly determine the ratio of homochirality to heterochirality to be approximately 5:5. One-dimensional stripe-like features with different orientations are observed in the heterochiral L/R stacking region, and the stripes are all along the $[211]$ direction of the underlying atomic lattice. This can be directly evidenced by the observed CDW states around the homochiral and heterochiral stacking edges in Figure 5j. Note that we can rule out the multiple-tip effect because it would have caused discontinuity in the surrounding CDW

unicells, while the unicells are smoothly connected in the above observation. The detailed mechanism for the formation of the nematic CDW states needs to be further investigated in conjunction with theoretical calculations, which is beyond the scope of this paper.

CONCLUSION

$1T$ -TaS₂ exhibits abundant physical properties and an electronic structure, providing an ideal platform to investigate the CDW order and strong electron–electron correlations. In the CCDW state, the central Mott electrons of SoDs form a flat-band structure at the E_F . This phenomenon is attributed to the interplay between electron–electron correlations and electron–lattice interactions. $1T$ -TaS₂ in the flat-band state demonstrates diverse quantum states, including superconductivity, CDW, and insulating states. The modulation of these quantum states is crucial for advancing our understanding of correlated electronic systems. Hole doping, as a particularly effective means of regulation, not only adjusts the flat-band filling factor in $1T$ -TaS₂ by altering the electron density but also induces changes in electronic interactions. This dual effect suggests a promising avenue for research aimed at realizing quantum states.

We directly visualize the filling-dependent stable multiple intertwined orders in $1T$ -TaS₂, involving hole order, phase domains, chiral domains, and mixed phase/chiral domains by STM (Figure S14). The evolution of intralayer electron correlations and interlayer CDW stacking order with a flat-band filling factor is further investigated in conjunction with DFT calculations. As the flat-band filling factor approaches 1, the system exhibits a long-range-ordered CCDW structure with some hole orders. As the flat-band filling factor decreases, phase and chiral domains of different shapes and sizes appear. As the flat-band filling factor further decreases, interlayer CDW stacking becomes progressively disordered, contributing to the weakening of interlayer interactions and the emergence of interlayer heterochiral stacking. The interplay of complex electron–electron correlations, electron–lattice interactions, and interlayer interactions collectively induces a redistribution of atoms into ring-SoD and stripe-SoD ordered structures, accompanied by a change in symmetry. This modulation of the atomic structure further feeds back into the electronic structure, complicating the interactions between the electronic and atomic orders. The study paves a way to realize exotic quantum states via the accurate tuning of interior interactions and flat-band filling factors in correlated materials. This approach to manipulating interactions and electronic degrees of freedom will inspire further research focus on electronic structures, properties, and applications in the field of correlated electron materials.

METHODS

Single-Crystal Growth of Ti-Doped $1T$ -TaS₂. The high-quality $1T$ -Ta_{1-x}Ti_xS₂ single crystals were grown by the chemical vapor transport (CVT) method. Ta (99.99%, Aladdin), TaCl₅ (99.99%, Aladdin), S (99.99%, Aladdin), and Ti (99.99%, Aladdin) powders with a nominal molar ratio of 1:0.02:2.05: x ($x = \sim 0.3\%$, 0.8%, 2.5%, 4.2%, 6.3%) were mixed thoroughly and then loaded into quartz tubes (inner diameter/outer diameter/length: 14/16/200 mm). Large $1T$ -Ta_{1-x}Ti_xS₂ crystals with sizes up to 10 mm were collected for further characterization and measurement. X-ray diffraction (XRD) and X-ray energy dispersive spectroscopy (EDS) were employed to determine the crystal structure, morphology, and composition of the as-prepared samples. The Ti-doping contents of all samples agree with their

nominal molar ratio of source materials, demonstrating the controllable synthesis. In order to visualize the filling factor of the flat bands more clearly for different doping concentrations, we approximate the filling factor n as the fraction.

Scanning Tunneling Microscopy (STM). High-quality Ti-doped 1T-TaS₂ crystals were cleaved at room temperature in ultrahigh vacuum at a base pressure of 2×10^{-10} Torr, and directly transferred to the cryogen-free variable-temperature STM system (PanScan Freedom, RHK). Chemically etched W tips were used for STM measurement in constant-current mode. The STM tips were calibrated on a clean Ag(111) surface. Gwyddion was used for the STM data analysis.

Density Functional Theory Calculations and Simulations. Our DFT calculations were performed using the generalized gradient approximation for the exchange-correlation potential, the projector augmented wave method, and a plane-wave basis set, as implemented in the Vienna *ab initio* simulation package (VASP). Dispersion correction was implemented using the DFT-D3 method with the PBE functional for the exchange potential. The effective U value of the on-site Coulomb interaction of the Ta d orbitals is 2.3 eV. All our simulation cells contain a 20 Å vacuum to prevent interlayer coupling between different layers. The plane-wave cutoff was set to 450 eV. A k -mesh of $5 \times 5 \times 1$ was adopted to sample the first Brillouin zone of the cell. Convergence is reached if the consecutive energy difference is within 10^{-5} eV for electronic iterations and the forces are less than 0.01 eV/Å.

ASSOCIATED CONTENT

Data Availability Statement

The authors declare that the data supporting the findings of this study are available within the article and its Supporting Information.

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsnano.4c13437>.

Details of STM, STS, and theoretical calculation results including interlayer and interlayer interactions, phase domain walls, chiral domain walls, ring-SoD, and stripe-SoD structures, etc. (PDF)

AUTHOR INFORMATION

Corresponding Authors

Wei Ji – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China; orcid.org/0000-0001-5249-6624; Email: wji@ruc.edu.cn

Weichang Zhou – Key Laboratory of Low-dimensional Quantum Structures and Quantum Control of Ministry of Education, School of Physics and Electronics, Institute of Interdisciplinary Studies, Hunan Normal University, Changsha 410081, People's Republic of China; orcid.org/0000-0003-3140-5951; Email: wchangzhou@hunnu.edu.cn

Zhihai Cheng – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872,

People's Republic of China; orcid.org/0000-0003-4938-4490; Email: zhihaicheng@ruc.edu.cn

Authors

Yanyan Geng – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China

Haoyu Dong – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China

Renhong Wang – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China

Jianfeng Guo – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China; Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Sciences, Beijing 100190, People's Republic of China

Shuo Mi – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China

Le Lei – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China; Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Sciences, Beijing 100190, People's Republic of China

Yan Li – Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Sciences, Beijing 100190, People's Republic of China

Li Huang – Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Sciences, Beijing 100190, People's Republic of China

Fei Pang – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics,

Renmin University of China, Beijing 100872, People's Republic of China; orcid.org/0000-0002-8578-366X

Rui Xu – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China

Weiqiang Yu – Key Laboratory of Quantum State Construction and Manipulation (Ministry of Education), Renmin University of China, Beijing 100872, People's Republic of China; Beijing Key Laboratory of Optoelectronic Functional Materials & Micro-nano Devices, Department of Physics, Renmin University of China, Beijing 100872, People's Republic of China

Hong-Jun Gao – Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Sciences, Beijing 100190, People's Republic of China; orcid.org/0000-0002-6766-0623

Complete contact information is available at:
<https://pubs.acs.org/10.1021/acsnano.4c13437>

Author Contributions

*Y.G., H.D., and R.W. contributed equally. W.J., H.G., W.Z. and Z.C. conceived the research project. Y.G., H.D., L.L., and Z.C. performed the STM experiments and analysis of STM data. J.G., S.M., Y.L., L.H., F.P., R.X., and W.Y. helped in the experiments. Y.G., H.D., W.Z., and Z.C. wrote the manuscript with input from all authors.

Notes

The authors declare no competing financial interest.

ACKNOWLEDGMENTS

This project was supported by the National Key R&D Program of China (MOST) (Grant No. 2023YFA1406500), the National Natural Science Foundation of China (NSFC) (Nos. 92477128, 92477205, 12374200, 11604063, 11974422, 12104504), the Strategic Priority Research Program (Chinese Academy of Sciences, CAS) (No. XDB30000000), and the Fundamental Research Funds for the Central Universities and the Research Funds of Renmin University of China (No. 21XNLG27). Y.Y. Geng was supported by the Outstanding Innovative Talents Cultivation Funded Programs 2023 of Renmin University of China. This paper is an outcome of “Study of Exotic Fractional Magnetization Plateau Phase Transitions and States in Low-dimensional Frustrated Quantum Systems” (RUC24QSDL039), funded by the “Qjushi Academic-Dongliang” Talent Cultivation Project at Renmin University of China in 2024.

REFERENCES

- (1) Chen, P.; Chan, Y.-H.; Fang, X.-Y.; Zhang, Y.; Chou, M. Y.; Mo, S.-K.; Hussain, Z.; Fedorov, A.-V.; Chiang, T.-C. Charge Density Wave Transition in Single-Layer Titanium Diselenide. *Nat. Commun.* **2015**, *6*, 8943.
- (2) Ugeda, M. M.; Bradley, A. J.; Zhang, Y.; Onishi, S.; Chen, Y.; Ruan, W.; Ojeda-Aristizabal, C.; Ryu, H.; Edmonds, M. T.; Tsai, H.-Z.; Riss, A.; Mo, S.-K.; Lee, D.; Zettl, A.; Hussain, Z.; Shen, Z.-X.; Crommie, M. F. Characterization of Collective Ground States in Single-Layer NbSe₂. *Nat. Phys.* **2016**, *12*, 92–97.
- (3) Ryu, H.; Chen, Y.; Kim, H.; Tsai, H.-Z.; Tang, S.; Jiang, J.; Liou, F.; Kahn, S.; Jia, C.; Omrani, A. A.; Shim, J. H.; Hussain, Z.; Shen, Z.-X.; Kim, K.; Min, B. I.; Hwang, C.; Crommie, M. F.; Mo, S.-K. Persistent Charge-Density-Wave Order in Single-Layer TaSe₂. *Nano Lett.* **2018**, *18*, 689–694.
- (4) Ye, J. T.; Zhang, Y. J.; Akashi, R.; Bahramy, M. S.; Arita, R.; Iwasa, Y. Superconducting Dome in a Gate-Tuned Band Insulator. *Science* **2012**, *338*, 1193–1196.
- (5) Rubio-Verdu, C.; Garcia-Garcia, A. M.; Ryu, H.; Choi, D.-J.; Zaldivar, J.; Tang, S.; Fan, B.; Shen, Z.-X.; Mo, S.-K.; Pascual, J. I.; Ugeda, M. M. Visualization of Multifractal Superconductivity in a Two-Dimensional Transition Metal Dichalcogenide in the Weak-Disorder Regime. *Nano Lett.* **2020**, *20*, 5111–5118.
- (6) Chen, Y.; Ruan, W.; Wu, M.; Tang, S.; Ryu, H.; Tsai, H.-Z.; Lee, R. L.; Kahn, S.; Liou, F.; Jia, C.; Albertini, O. R.; Xiong, H.; Jia, T.; Liu, Z.; Sobota, J. A.; Liu, A. Y.; Moore, J. E.; Shen, Z.-X.; Louie, S. G.; Mo, S.-K. Strong Correlations and Orbital Texture in Single-Layer 1T-TaSe₂. *Nat. Phys.* **2020**, *16*, 218–224.
- (7) Bonilla, M.; Kolekar, S.; Ma, Y.; Diaz, H. C.; Kalappattil, V.; Das, R.; Eggers, T.; Gutierrez, H. R.; Phan, M.-H.; Batzill, M. Strong Room-Temperature Ferromagnetism in VSe₂ Monolayers on van der Waals Substrates. *Nat. Nanotechnol.* **2018**, *13*, 289–293.
- (8) Anshul, K.; Melinda, S. R.; Sean, V.; Ali, A. H.; Felix, F.; Young, I. J.; Luc, V.; Greg, J. M.; Tai, C. C.; Eduardo, F.; et al. Signatures of exciton condensation in a transition metal dichalcogenide. *Science* **2017**, *358* (6368), 1314–1317.
- (9) Rosnagel, K. On the origin of charge-density waves in select layered transition-metal dichalcogenides. *J. Phys.: Condens. Matter* **2011**, *23*, 213001.
- (10) Zhong, Y. G.; Liu, J. J.; Wu, X. X.; Guguchia, Z.; Yin, J.-X.; Mine, A.; Li, Y. K.; Najafzadeh, S.; Das, D.; Mielke, C.; Khasanov, R.; Luetkens, H.; Suzuki, T.; Liu, K. C.; Han, X. L.; Kondo, T.; Hu, J. P.; Shin, S.; Wang, Z. W.; Shi, X.; Yao, Y. G.; Okazaki, K. Nodeless electron pairing in CsV₃Sb₅ derived kagome superconductors. *Nature* **2023**, *617*, 488–492.
- (11) Li, C. S.; Xu, F.; Li, B. H.; Li, J. Y.; Li, G.; Watanabe, K. J.; Taniguchi, T.; Tong, B. B.; Shen, J.; Lu, L.; Jia, J. F.; Wu, F. C.; Liu, X. X.; Li, T. X. Tunable superconductivity in electron- and hole-doped Bernal bilayer graphene. *Nature* **2024**, *631*, 300–306.
- (12) Cao, Y.; Park, J. M.; Watanabe, K. J.; Taniguchi, T.; Jarillo-Herrero, P. Pauli-limit violation and re-entrant superconductivity in moiré graphene. *Nature* **2021**, *595*, 526–531.
- (13) Zhang, Y.; Yang, L. X.; Xu, M.; Ye, Z. R.; Chen, F.; He, C.; Xu, H. C.; Jiang, J.; Xie, B. P.; Ying, J. J.; Wang, X. F.; Chen, X. H.; Hu, J. P.; Matsunami, M.; Kimura, S.; Feng, D. L. Nodeless superconducting gap in AxFe₂Se₂ (A = K, Cs) revealed by angle-resolved photoemission spectroscopy. *Nat. Mater.* **2011**, *10*, 273–277.
- (14) Li, X.; Changwei, Z.; Ding, Y.; Yan, H.; Ye, S.; Li, H.; Hao, Z.; Zhao, L.; Zhou, X.; Wang, Y. Evolution of Charge and Pair Density Modulations in Overdoped Bi₂Sr₂CuO_{6+δ}. *Phys. Rev. X* **2021**, *11*, 011007.
- (15) Wise, W.; Boyer, M.; Chatterjee, K.; Kondo, T.; Takeuchi, T.; Ikuta, H.; Wang, Y. Y.; Hudson, E. W. Charge-density-wave origin of cuprate checkerboard visualized by scanning tunnelling microscopy. *Nat. Phys.* **2008**, *4*, 696–699.
- (16) Cao, L.; Xue, Y.; Wang, Y.; Zhang, F.-C.; Kang, J.; Gao, H.-J.; Mao, J.; Jiang, Y. Directly visualizing nematic superconductivity driven by the pair density wave in NbSe₂. *Nat. Commun.* **2024**, *15* (1), 7234.
- (17) Wen, C. H. P.; Xu, H. C.; Chen, C.; Huang, Z. C.; Lou, X.; Pu, Y. J.; Song, Q.; Xie, B. P.; Abdel-Hafiez, M.; Chareev, D. A.; et al. Anomalous correlation effects and unique phase diagram of electron-doped FeSe revealed by photoemission spectroscopy. *Nat. Commun.* **2016**, *7* (1), 10840.
- (18) Chen, F.; Xu, M.; Ge, Q. Q.; Zhang, Y.; Ye, Z. R.; Yang, L. X.; Jiang, J.; Xie, B. P.; Che, R. C.; Zhang, M.; Wang, A. F.; Chen, X. H.; Shen, D. W.; Hu, J. P.; Feng, D. L. Electronic Identification of the Parental Phases and Mesoscopic Phase Separation of K_xFe_{2-y}Se₂ Superconductors. *Phys. Rev. X* **2011**, *1*, 021020.
- (19) Yi, M.; Lu, D. H.; Yu, R.; Riggs, S. C.; Chu, J.-H.; Lv, B.; Liu, Z. K.; Lu, M.; Cui, Y.-T.; Hashimoto, M.; Mo, S.-K.; Hussain, Z.; Chu, C. W.; Fisher, I. R.; Si, Q.; Shen, Z.-X. Observation of Temperature-

Induced Crossover to an Orbital-Selective Mott Phase in $AxFe_3Se_2$ ($A = K, Rb$) Superconductors. *Phys. Rev. Lett.* **2013**, *110*, 067003.

(20) Kang, Y. M.; Najmaei, S.; Liu, Z.; Bao, Y. J.; Wang, Y. M.; Zhu, X.; Halas, N. J.; Nordlander, P.; Ajayan, P. M.; Lou, J.; Fang, Z. Y. Plasmonic hot electron induced structural phase transition in a MoS_2 monolayer. *Adv. Mater.* **2014**, *26*, 6467–6471.

(21) Lin, Y.-C.; Torsi, R.; Geohegan, D. B.; Robinson, J. A.; Xiao, K. Controllable Thin-Film Approaches for Doping and Alloying Transition Metal Dichalcogenides Monolayers. *Adv. Sci.* **2021**, *8* (9), 2004249.

(22) Lee, S.-H.; Goh, J. S.; Cho, D. Origin of the insulating phase and first-order metal-insulator transition in $1T-TaS_2$. *Phys. Rev. Lett.* **2019**, *122*, 106404.

(23) Wilson, J. A.; Di Salvo, F. J.; Mahajan, S. Charge-density waves in metallic, layered, transition-metal dichalcogenides. *Phys. Rev. Lett.* **1974**, *32*, 882–885.

(24) Geng, Y. Y.; Lei, L.; Dong, H. Y.; Guo, J. F.; Mi, S.; Li, Y.; Huang, L.; Pang, F.; Xu, R.; Zhou, W. C.; Liu, Z.; Ji, W.; Cheng, Z. H. Hysteretic electronic phase transitions in correlated charge-density-wave state of $1T-TaS_2$. *Phys. Rev. B* **2023**, *107*, 195401.

(25) Butler, C. J.; Yoshida, M.; Hanaguri, T.; Iwasa, Y. Mottness versus unit-cell doubling as the driver of the insulating state in $1T-TaS_2$. *Nat. Commun.* **2020**, *11* (1), 2477.

(26) Ritschel, T.; Berger, H.; Geck, J. Stacking-driven gap formation in layered $1T-TaS_2$. *Phys. Rev. B* **2018**, *98*, 195134.

(27) Lee, J.; Jin, K. H.; Yeom, H. W. Distinguishing a Mott Insulator from a Trivial Insulator with Atomic Adsorbates. *Phys. Rev. Lett.* **2021**, *126*, 196405.

(28) Wang, Z. L.; Dong, H. Y.; Zhou, W. C.; Cheng, Z. H.; Wang, S. C. Flat band in hole-doped transition metal dichalcogenide observed by angle-resolved photoemission spectroscopy. *Chin. Phys. B* **2023**, *32*, 067103.

(29) Geng, Y. Y.; Guo, J. F.; Meng, F. Y.; Wang, M. Y.; Mi, S.; Huang, L.; Xu, R.; Pang, F.; Liu, K.; Wang, S. C.; Gao, H.-G.; Zhou, W. C.; Ji, W.; Lei, H. C.; Cheng, Z. H. Correlated electrons of the flat band in charge density wave state of $4H_b-TaSe_{2-x}$. *Phys. Rev. B* **2024**, *110*, 115107.

(30) Bang, J.; Lee, B.; Yang, H.; Kim, S.; Wulferding, D.; Cho, D. Charge-ordered phases in the hole-doped triangular Mott insulator $4H_b-TaS_2$. *Phys. Rev. B* **2024**, *109*, 195170.

(31) Lee, D.; Jin, K.-H.; Feng, L.; Yeom, H. W. Tunable Mott Dirac and Kagome bands engineered on $1T-TaS_2$. *Nano Lett.* **2022**, *22* (19), 7902–7909.

(32) Zhang, W.; Gao, J.; Cheng, L.; Bu, K.; Wu, Z.; Fei, Y.; Zheng, Y.; Wang, L.; Li, F.; Luo, X.; et al. Visualizing the evolution from Mott insulator to Anderson insulator in Ti-doped $1T-TaS_2$. *npj Quantum Mater.* **2022**, *7* (1), 8.

(33) Patel, R. K.; Patra, K.; Ojha, S. K.; Kumar, S.; Sarkar, S.; Saha, A.; Bhattacharya, N.; Freeland, J. W.; Kim, J.-W.; Ryan, P. J.; et al. Hole doping in a negative charge transfer insulator. *Commun. Phys.* **2022**, *5* (1), 216.

(34) Cho, D.; Cheon, S.; Kim, K.-S.; Lee, S.-H.; Cho, Y.-H.; Cheong, Y.; W, H. Nanoscale manipulation of the Mott insulating state coupled to charge order in $1T-TaS_2$. *Nat. Commun.* **2016**, *7* (1), 10453.

(35) Cho, D.; Gye, G.; Lee, J.; Lee, S.-H.; Wang, L. H.; Cheong, S.-W.; Yeom, H. W. Correlated electronic states at domain walls of a Mott-charge-density-wave insulator $1T-TaS_2$. *Nat. Commun.* **2017**, *8* (1), 392.

(36) Ma, L.; Ye, C.; Yu, Y.; Lu, X. F.; Niu, X.; Kim, S.; Feng, D.; Tománek, D.; Son, Y.-W.; Chen, X. H.; et al. A metallic mosaic phase and the origin of Mott-insulating state in $1T-TaS_2$. *Nat. Commun.* **2016**, *7* (1), 10956.

(37) Bu, K.; Zhang, W.; Fei, Y.; Wu, Z.; Zheng, Y.; Gao, J.; Luo, X.; Sun, Y.-P.; Yin, Y. Possible strain induced Mott gap collapse in $1T-TaS_2$. *Commun. Phys.* **2019**, *2* (1), 146.

(38) Zhang, J.; Lian, C.; Guan, M. X.; Ma, W.; Fu, H. X.; Guo, H. Z.; Meng, S. Photoexcitation induced quantum dynamics of charge

density wave and emergence of a collective mode in $1T-TaS_2$. *Nano Lett.* **2019**, *19*, 6027–6034.

(39) Ohta, S.; Kobayashi, S.; Nomura, A.; Sakata, H. Electronic state modulation of the Star of David lattice by stacking of $\sqrt{13} \times \sqrt{13}$ domains in $1T-TaSe_2$. *Phys. Rev. B* **2021**, *104*, 155433.

(40) Jarc, G.; Mathengattil, S. Y.; Montanaro, A.; Giusti, F.; Rigoni, E. M.; Sergio, R.; Fassioli, F.; Winnerl, S.; Zilio, S. D.; Mihailovic, D.; et al. Cavity-mediated thermal control of metal-to-insulator transition in $1T-TaS_2$. *Nature* **2023**, *622* (7983), 487–492.

(41) Park, J. W.; Lee, J. W.; Yeom, H. W. Zoology of domain walls in quasi-2D correlated charge density wave of $1T-TaS_2$. *npj Quantum Mater.* **2021**, *6* (1), 32.

(42) Song, X.; Liu, L.; Chen, Y.; Yang, H.; Huang, Z.; Hou, B.; Hou, Y.; Han, X.; Yang, H.; Zhang, Q.; et al. Atomic-Scale Visualization of Chiral Charge Density Wave Superlattices and Their Reversible Switching. *Nat. Commun.* **2022**, *13* (1), 1843.

(43) Liu, L. W.; Song, X.; Dai, J. Q.; Yang, H.; Chen, Y. Y.; Huang, X. Y.; Huang, Z. P.; Ji, H. Y.; Zhang, Y.; Wu, X.; Sun, J.-T.; Zhang, Q. Z.; Zhou, J. D.; Huang, Y.; Qiao, J. S.; Ji, W.; Gao, H.-J.; Wang, Y. L. Unveiling Electronic Behaviors in Heterochiral Charge-Density-Wave Twisted Stacking Materials with 1.25 nm Unit Dependence. *ACS Nano* **2023**, *17*, 2702–2710.

(44) Ravnik, J.; Vaskivskiy, Y.; Vodeb, J.; Diego, M.; Venturini, R.; Gerasimenko, Y.; Kabanov, V.; Kranjec, A.; Mihailovic, D. Chiral domain dynamics and transient interferences of mirrored superlattices in nonequilibrium electronic crystals. *Sci. Rep.* **2023**, *13* (1), 19622.

(45) Geng, Y. Y.; Dong, H. Y.; Wang, R. H.; Gu, J. F.; Mi, S.; Lei, L.; Li, Y.; Huang, L.; Pang, F.; Xu, R. et al. Filling-dependent intertwined electronic and atomic orders in the flat-band state of $1T-TaS_2$. *arXiv*, **2025**.