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## Orbital-Ordering Driven Simultaneous Tunability of Magnetism and Electric Polarization in Strained Monolayer $VCl_3$

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Two-dimensional (2D) van der Waals magnetic materials have promising and versatile electronic and magnetic properties in the 2D limit, indicating a considerable potential to advance spintronic applications. Theoretical predictions thus far have not ascertained whether monolayer  $VCl_3$  is a ferromagnetic (FM) or anti-FM monolayer; this also remains to be experimentally verified. We theoretically investigate the influence of potential factors, including  $C_3$  symmetry breaking, orbital ordering, epitaxial strain, and charge doping, on the magnetic ground state. Utilizing first-principles calculations, we predict a collinear type-III FM ground state in monolayer  $VCl_3$  with a broken  $C_3$  symmetry, wherein only the former two of three  $t_{2g}$  orbitals ( $a_{1g}$ ,  $e_{g2}^\pi$  and  $e_{g1}^\pi$ ) are occupied. The atomic layer thickness and bond angles of monolayer  $VCl_3$  undergo abrupt changes driven by an orbital ordering switch, resulting in concomitant structural and magnetic phase transitions. Introducing doping to the underlying Cl atoms of monolayer  $VCl_3$  without  $C_3$  symmetry simultaneously induces in- and out-of-plane polarizations. This can achieve a multiferroic phase transition if combined with the discovered adjustments of magnetic ground state and polarization magnitude under strain. The establishment of an orbital-ordering driven regulatory mechanism can facilitate deeper exploration and comprehension of magnetic properties of strongly correlated systems in monolayer  $VCl_3$ .

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Two-dimensional (2D) magnetic materials have recently garnered substantial attention because of their promising applications in spintronics,<sup>[1–4]</sup> including magnetic logical devices,<sup>[5–7]</sup> storage,<sup>[8]</sup> and sensors.<sup>[9]</sup> The discovery of the first monolayer ferromagnetic (FM)  $CrI_3$  in 2017<sup>[7]</sup> has paved the way for continuous experimental confirmations of monolayer magnets, such as  $Fe_3GeTe_2$ ,<sup>[10]</sup>  $CrOCl$ ,<sup>[11]</sup>  $CrSBr$ ,<sup>[12,13]</sup>  $CrTe_2$ ,<sup>[14]</sup> and  $CrSe_2$ ,<sup>[15]</sup> substantially augmenting the diversity of available 2D magnets. In addition to various strategies for tuning interlayer magnetism,<sup>[16–19]</sup> intralayer magnetism within a monolayer magnet can be modified through approaches such as breaking geometric symmetry,<sup>[20]</sup> applying in-plane (IP) strain,<sup>[21]</sup> and introducing electric doping.<sup>[22]</sup> Moreover, orbital ordering in open-shell magnetic cations can add a new dimension to the tunability of intralayer magnetism.<sup>[23]</sup>

The V cation in 2D vanadium trihalides  $VX_3$  ( $X = Cl, Br, \text{ or } I$ ) is an open-shell cation with a valence of  $3+$ , leaving two  $3d$  electrons to fill three  $t_{2g}$  orbitals. These originally degenerate triplet  $t_{2g}$  orbitals split into a singlet ( $a_{1g}$ ) and doublet ( $e_g^\pi$ ) owing to the presence of a triangular crystal field.<sup>[23–25]</sup> Despite variations in their orbital orderings,<sup>[23,24]</sup> both  $VI_3$  and  $VBr_3$  monolayers have been identified as FM insulators. However, the magnetic ground state of  $VCl_3$  remains indeterminate between those of an FM Dirac semimetal<sup>[26,27]</sup> and a zigzag (ZZ) anti-FM (AFM) semiconductor.<sup>[28]</sup> Hence, subtle tunability among different magnetic configurations of monolayer  $VCl_3$  may exist, implying a potential FM/AFM transition under external perturbations. Moreover, a magnetic transition driven by the alteration of orbital orderings is often associated with structural symmetry variations,<sup>[29,30]</sup> such as the elimination or introduction of structural inversion

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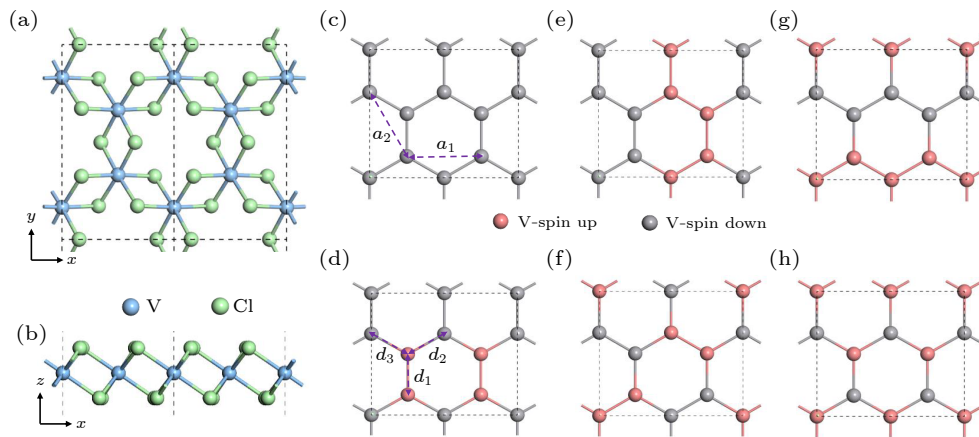
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or  $C_3$  rotational symmetry. This may lead to simultaneous variations in electric polarization and magnetization.

In this work, we theoretically explored the tunability of the magnetic and electric polarization properties in monolayer  $VCl_3$  subjected to uniaxial strain and charge doping, with orbital ordering serving as the driving mechanism. Our analysis encompassed 18 configurations from three structural classifications and six magnetic orders for the  $VCl_3$  monolayer. An FM semiconducting state characterized by the absence of IP  $C_3$  rotational symmetry is the global ground state for the strain-free monolayer  $VCl_3$ . For simplicity, we adopted the FM configuration with  $C_3$  symmetry as the strain-free reference configuration. Then, we modulated the magnetic properties of monolayer  $VCl_3$  under uniaxial epitaxial  $x$ -strain, which is correlated with geometric structures and orbital ordering. We further examined the electric polarization properties of strained monolayer  $VCl_3$  under electron doping, which can induce out-of-plane (OOP) and IP electric polarization. In addition, uniaxial  $y$ -axis strain and biaxial epitaxial strains were considered.

We performed density functional theory calculations using the generalized gradient approximation for the exchange-correlation potential,<sup>[31]</sup> projector augmented wave method,<sup>[32,33]</sup> and a plane-wave basis set, as implemented in Vienna *ab initio* simulation package (VASP).<sup>[34,35]</sup> In addition, dispersion correction was achieved using Grimme's D3 form PBE-D3.<sup>[31,36]</sup> Moreover, to account for on-site Coulomb interactions within the V  $3d$  orbitals, the DFT + U method<sup>[37]</sup> was applied

with an effective  $U$  value of 3.0 eV, which was similar to that used in other studies.<sup>[20,26,38]</sup> The cut-off kinetic energy for the plane-wave basis set was set to 700 eV in both structural relaxations and total energy calculations. All the geometric structures were fully relaxed until the residual force per atom was less than 0.005 eV/Å. A  $2 \times \sqrt{3} \times 1$  rectangular supercell was used to compare the total energies of different magnetic configurations, ensuring energy comparisons under the same conditions. A  $7 \times 9 \times 1$   $k$ -mesh was adopted to sample the Brillouin zone of the  $2 \times \sqrt{3} \times 1$  supercell. A vacuum layer over 15 Å in thickness was adopted to eliminate interactions among image slabs. Uniaxial epitaxial strains along the  $x(y)$  axis were applied to the FM structure of monolayer  $VCl_3$  (with  $C_3$  symmetry) by varying the lattice constant along the  $x(y)$  axis while maintaining it along the  $y(x)$  axis. Biaxial strains were also implemented by assigning certain sets of  $x$  and  $y$  lattice constants to the monolayer. Charge doping was achieved through the ionic potential method,<sup>[39]</sup> which ensured the neutrality of the supercell and confined exceeding electrons around the doped atoms. The Cl  $2s$  orbital core potential was modified<sup>[40]</sup> to accumulate the doped electrons on Cl atoms in the bottom sublayer. The electric polarizations were derived using the Berry phase method.<sup>[41]</sup> The thickness of the atomic layer ( $h$ ) was quantified by identifying the highest and lowest positions of the Cl atoms in monolayer  $VCl_3$ . As the  $\theta_1$  values were identical for different octahedral under uniaxial strain along the  $x$  axis, only one  $\theta_1$  value was evaluated under different strains.



**Fig. 1.** (a) Top and (b) side views of fully relaxed geometric structure of monolayer  $VCl_3$  in  $1 \times \sqrt{3} \times 1$  supercell. The light blue and green balls represent V and Cl atoms, respectively. Illustrations of (c) FM, (d) bi-stripe-AFM state, (e) armchair-AFM state, (f) bi-Néel-AFM state, (g) ZZ-AFM state, and (h) Néel-AFM state. The gray and pink balls represent up and down majority spins of V atoms, respectively. Variables  $d_1$ ,  $d_2$ , and  $d_3$  ( $a_1$  and  $a_2$ ) denote the nearest (second-nearest) neighbor V-V distances along three (two) directions.

Freestanding monolayer  $VCl_3$  exhibited geometric similarities with monolayer  $CrX_3$  ( $X = Cl, Br, \text{ or } I$ ), where  $M-Cl$  ( $M = V \text{ or } Cr$ ) octahedra shared common edges and coalesced into a hexagonal monolayer that displayed IP  $C_3$  rotational symmetry. Figures 1(a) and 1(b) show the top and side views of the monolayer  $VCl_3$  atomic structure

within two rectangular  $1 \times \sqrt{3}$  supercells. Figures 1(c)–1(h) show the six magnetic orders considered for each structural category in rectangular  $2 \times \sqrt{3}$  supercells to ascertain the magnetic ground state. The three nearest-neighbor V-V atomic distances, denoted as  $d_1$ – $d_3$  [see Fig. 1(d)], divide the fully relaxed geometric structures into three categories,

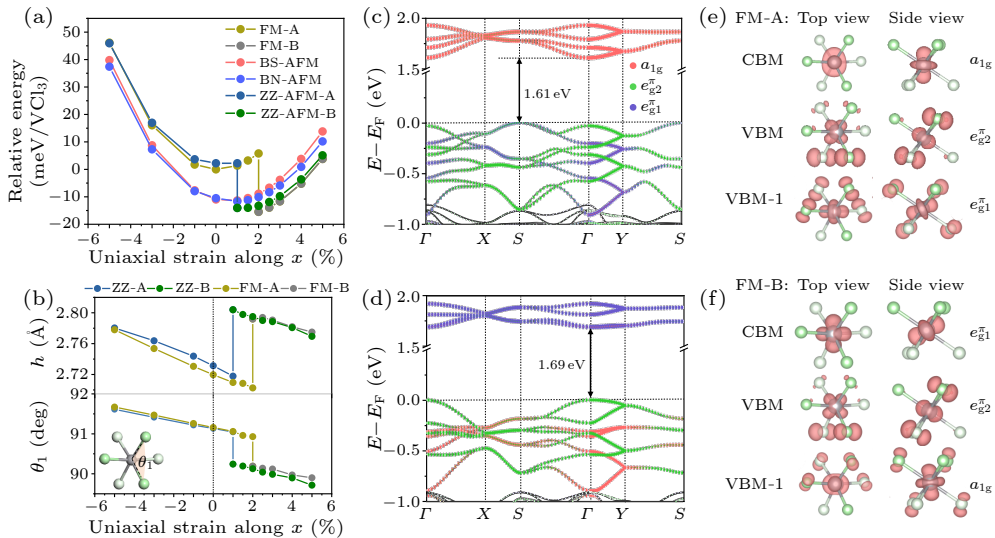
as listed in Table 1. While the  $C_3$  rotational symmetry is nearly preserved in type-I structures, the symmetry breaks in both type-II and type-III structures. The critical distinction between type-II and type-III structures lies in whether  $d_1$  is smaller (type-II) or larger (type-III) than  $d_2$  and  $d_3$ .

Among all the type-I configurations with (nearly) preserved  $C_3$  rotational symmetry, the FM state is the energetically favored configuration, exhibiting lattice constant  $a = 6.092 \text{ \AA}$ , equivalent to  $d_1 = d_2 = d_3 = 3.517 \text{ \AA}$ . The breakdown of the  $C_3$  symmetry results in a lower energy state for most magnetic configurations within the type-II and III categories, as indicated by their reduced total energies compared with their type-I counterparts (see Table 1). Only three (type-II) and four (type-III) magnetic configurations are listed in Table 1 because not all mag-

netic orders could be obtained in structures with broken  $C_3$  symmetry. Remarkably, the global ground state is type-III FM characterized by lattice constants  $a_1 = 6.156 \text{ \AA}$ ,  $a_2 = 6.105 \text{ \AA}$ ,  $d_1 = 3.543 \text{ \AA}$ , and  $d_2 = d_3 = 3.530 \text{ \AA}$ . The second most stable configuration is type-III ZZ AFM, which is  $2.6 \text{ meV/VCl}_3$  less stable than type-III FM. The stability of monolayer  $\text{VCl}_3$  is substantially influenced by the preservation of  $C_3$  symmetry. Despite minor numerical differences in V-V distances between the type-I and type-III FM configurations, a large energy difference of  $16.6 \text{ meV/VCl}_3$  is observed. Given the nearly identical atomic structures and consistent FM order, this difference implies that the orbital ordering most likely plays a paramount role ascribed to the open-shell V cation in monolayer  $\text{VCl}_3$ .

**Table 1.** Structural parameters and total energies of six magnetic configurations. Here  $a_1$  and  $a_2$  are the distances between the next-nearest-neighbor V atoms, and  $d_1$ – $d_3$  are the distances between the nearest-neighbor V atoms [marked in Figs. 1(c) and 1(d)].

	Magnetic configuration	$a_1$ (Å)	$a_2$ (Å)	$d_1$ (Å)	$d_2$ (Å)	$d_3$ (Å)	Energy (meV/ $\text{VCl}_3$ )	$C_3$ symmetry
Type-I	FM	6.092	6.092	3.517	3.517	3.517	16.6	Yes (Nearly)
	ZZ-AFM	6.086	6.089	3.510	3.517	3.517	18.8	
	AC-AFM	6.089	6.090	3.517	3.513	3.516	19.0	
	BS-AFM	6.089	6.088	3.516	3.514	3.514	22.4	
	BN-AFM	6.087	6.088	3.515	3.515	3.515	22.3	
	Néel AFM	6.067	6.067	3.503	3.503	3.503	518.8	
Type-II	FM	6.155	6.106	3.526	3.539	3.539	18.1	No ( $d_1 < d_2, d_3$ )
	BN-AFM	6.099	6.117	3.515	3.532	3.536	5.7	
	Néel AFM	6.098	6.113	3.519	3.530	3.530	7.3	
Type-III	FM	6.156	6.105	3.543	3.530	3.530	0	No ( $d_1 > d_2, d_3$ )
	ZZ-AFM	6.163	6.110	3.555	3.529	3.529	2.6	
	BS-AFM	6.121	6.100	3.534	3.522	3.522	5.1	
	Néel AFM	6.127	6.102	3.536	3.524	3.524	6.8	



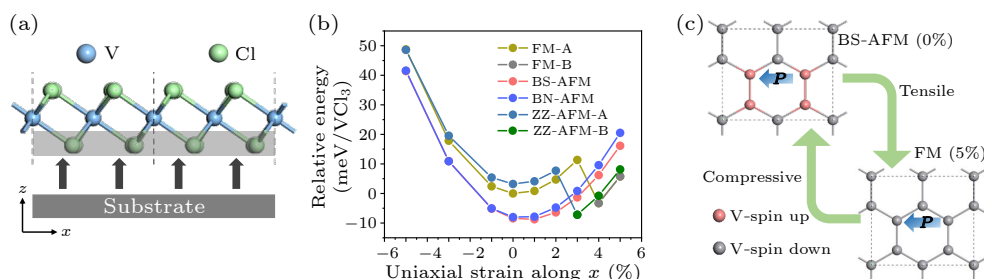
**Fig. 2.** (a) Energy–strain relation under uniaxial strain along the  $x$  axis in FM state (gray and olive) as well as bi-stripe-AFM state (red), bi-Néel-AFM state (royal blue), and ZZ-AFM (green and dark blue) state. The energy of the strain-free type-I FM configuration is chosen as the zero-energy reference. (b) Variations in layer thickness  $h$  and Cl–V–Cl angle  $\theta_1$  under uniaxial  $x$ -axis strain in FM and ZZ-AFM orders. (c) FM-A and (d) FM-B under 2% uniaxial  $x$ -axis strain. Plots of wavefunction norms for conduction band minimum (CBM), valence band maximum (VBM), and VBM-1 (i.e., band below VBM) state at the  $\Gamma$  point of (e) FM-A and (f) FM-B under 2%  $x$ -axis strain. The isosurface values are set to  $2 \times 10^{-3} e/\text{Bohr}^3$ .

Uniaxial epitaxial strain was applied to the fully relaxed  $2 \times \sqrt{3} \times 1$  type-I FM supercell along the  $x$  or  $y$  axis, in which three magnetic transitions were observed. Figure 2(a) shows the total energies of the bi-stripe (BS)-AFM, bi-Néel (BN)-AFM, ZZ-AFM, and FM orders under uniaxial  $x$ -axis strain in the range of  $\pm 5\%$ . We employed the strain-free type-I FM configuration as the reference lattice (0.0%) to evaluate the strain effects. Under 0% strain lattice, the BN-AFM (royal blue dots) and BS-AFM (red dots) configurations, which lack  $C_3$  structural symmetry, are more stable than the FM configuration by 10.5 and 11.0 meV/VCl<sub>3</sub>, respectively [Fig. 2(a)]. The BN-AFM order becomes the magnetic ground state for  $x$ -axis compressive strain exceeding 1%. For tensile strains, the energy of the ZZ-AFM order drops below those of the BN- and BS-AFM orders at 1%  $x$ -axis tensile strain, becoming the global ground state. Further increasing the tensile strain to 2% abruptly reduces the energy of the FM order, and the ground state shifts to another FM state. The FM state maintains its superior stability up to at least 5%  $x$ -axis strain, indicating that the magnetic ground state transforms from BN-AFM to ZZ-AFM and then to FM under epitaxial tensile strain along the  $x$  axis.

The abrupt variation in energies indicate the existence of two categories of ZZ-AFM (FM) configurations, which were characterized by orbital ordering, as detailed below. The ZZ-AFM (FM) state before the abrupt variation is termed as set A comprising the ZZ-AFM-A and FM-A states, whereas set B comprises the ZZ-AFM-B and FM-B states after that abrupt variation. The ZZ-AFM-A/ZZ-AFM-B transition is indicative of an abrupt increase of approximately 0.1 Å in the atomic layer thickness  $h$  and decrease in angle  $\theta_1$  of approximately  $1^\circ$  under 1% tensile strain [Fig. 2(b)], with a corresponding negative Poisson's ratio ( $-5.9$ ) during the transition. This anomalous structural change is similarly observed in the FM-A/FM-B transition at 2% tensile  $x$ -axis strain. Moreover, this structural alternation coincides with a transition from an indirect [1.61 eV, FM-A, Fig. 2(c)] to a direct [1.69 eV, FM-B, Fig. 2(d)] bandgap. This abrupt change in both the bandgap value and band dispersion suggests a substantial electronic structure alternation, signaling a rearrangement

in the ordering of the  $t_{2g}$  orbitals. To examine the orbital orderings, we projected the band structures onto the one  $a_{1g}$  and two  $e_g^\pi$  orbitals [Figs. 2(c) and 2(d)]. The projections demonstrate that these two FM states possess different orbital orderings, where  $a_{1g}$  (red) and  $e_{g1}^\pi$  (violet) are unoccupied in FM-A and FM-B, respectively. The wavefunction norms of these states plotted around the bandgap at the  $\Gamma$  point are shown in Figs. 2(e) and 2(f). Their shapes and energy levels corroborate the orbital orderings inferred from the band structure projections [Figs. 2(c) and 2(d)].

Then, we elucidated the mechanism underlying the changes in orbital ordering induced by  $x$ -axis strain. Upon stretching along the  $x$  axis, both the layer thickness ( $h$ ) and Cl-V-Cl bond angle ( $\theta_1$ ) initially decrease [Fig. 2(b)], prompting the V-Cl bonds to approach closer to the plane of the V  $e_{g1}^\pi$  orbital. This gradual reduction in the octahedral space promotes the wavefunction to overlap between the V-Cl  $\sigma$ -bonding state and  $e_{g1}^\pi$  orbital. This strengthened non-bonding wavefunction overlap enhances the Pauli and Coulomb repulsions between the V-Cl  $\sigma$ -bonding state and  $e_{g1}^\pi$  orbital, rendering the  $e_{g1}^\pi$  orbital less stable upon lattice stretching. A transition characterized by an intersection of the orbital energies occurs at approximately 2%  $x$ -axis strain, resulting in the  $e_{g1}^\pi$  orbital becoming unoccupied as the progressively intensified repulsion elevates it above the Fermi level. Thus, the initially unoccupied  $a_{1g}$  orbital in FM-A [Fig. 2(e)] reaches a lower energy state and becomes occupied in FM-B [Fig. 2(f)] owing to the abrupt increase in the atomic layer thickness. The increased thickness ( $h$ ) in FM-B provides additional space within the V-Cl octahedron, drastically reducing the repulsion between the  $a_{1g}$  orbital and V-Cl bonding state, thereby reducing the  $a_{1g}$  orbital energy and rendering it occupied. These results indicate that strain-induced alterations in the electronic structure and magnetism of monolayer VCl<sub>3</sub> are governed by changes in orbital orderings. Therefore, a new dimension for tuning the electronic and magnetic properties of VCl<sub>3</sub> becomes available through epitaxial strain; tuning can also be achieved by charge doping, as discussed in the following.

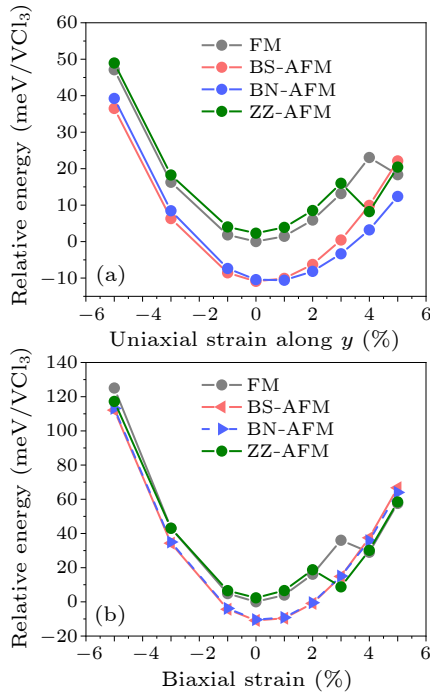


**Fig. 3.** (a) Schematic of epitaxial strain and doping between substrate and monolayer VCl<sub>3</sub>. (b) Energy-strain relation under uniaxial strain along  $x$  axis and doping with 0.01  $e^-$ /Cl of bottom layer in FM as well as BS-AFM, BN-AFM, and ZZ-AFM states. The energy reference is consistent with that adopted in Fig. 2, namely, the total energy of the strain-free type-I FM configuration. (c) Transition between BS-AFM and FM states under  $x$ -axis strain and doping.



When a 2D material epitaxially grows on a substrate, charge transfers often coexist at the interface with epitaxial strain. To model this charge doping effect, we introduced  $0.01 e/\text{Cl}$  doping to the bottom Cl atoms of monolayer  $\text{VCl}_3$  and explored the magnetic properties under uniaxial  $x$ -axis strain. As shown in Fig. 3(b), this uniform doping does not change the magnetic ground state of the strain-free lattice. The BS-AFM order maintains its superior stability under 0% uniaxial  $x$ -axis strain. As the  $x$ -axis strain increases to 3%, the ZZ-AFM-B order becomes the magnetic ground state [Fig. 3(b)]. A ZZ-AFM-B to FM-B magnetic transition occurs when the  $x$ -axis tensile strain increases to 4%. The results indicate that charge doping does not qualitatively change the sequence of strain induced magnetic transitions, but shifts the critical strains to higher values.

Charge doping from the substrate has been reported to break the inversion symmetry in monolayer  $\text{CrI}_2$ , leading to IP polarization.<sup>[42]</sup> In this study, charge doping on the interfacial Cl layer of type-I FM breaks the structural inversion symmetry, resulting in an OOP electric polarization. A  $0.01 e/\text{Cl}$ -doped type-I FM monolayer  $\text{VCl}_3$  retaining  $C_3$  symmetry exhibits OOP electric polarization of  $0.03 \mu\text{C}/\text{cm}^2$ ; this value highly depends on the doping level. For instance, a higher doping level increases the electric polarization. In particular, OOP polarization increases to  $0.12 \mu\text{C}/\text{cm}^2$  in a  $0.10 e/\text{Cl}$ -doped type-I FM monolayer.



**Fig. 4.** (a) Energy–strain relationship under uniaxial strain along  $y$  axis in FM (gray) as well as BS-AFM (red), BN-AFM (blue), and ZZ-AFM (green) states. (b) Energy–strain relationship under biaxial strain in FM as well as BS-AFM, BN-AFM, and ZZ-AFM states. The energy reference is consistent with that adopted in Figs. 2 and 3, namely, the total energy of the strain-free type-I FM configuration.

When the  $C_3$  symmetry of monolayer  $\text{VCl}_3$  is compromised (e.g., in the type-III FM configuration), the inversion symmetry is retained in the absence of charge doping. If the inversion symmetry is previously compromised in monolayer  $\text{VCl}_3$  by, for example, charge doping, the breakdown of IP  $C_3$  rotational symmetry additionally introduces an IP electric polarization. For  $0.01 e/\text{Cl}$ -doped BS-AFM monolayer  $\text{VCl}_3$  lacking  $C_3$  symmetry, an IP polarization of  $0.012 \mu\text{C}/\text{cm}^2$  appears along the  $x$  axis in addition to an OOP polarization of  $0.009 \mu\text{C}/\text{cm}^2$ . In addition to inducing a magnetic phase transition, an increased strain typically increases the polarization value. For instance, the magnetic ground state transitions to the FM-B configuration under 5% uniaxial  $x$ -axis strain, and the IP polarization along the  $x$ -axis increased to  $0.016 \mu\text{C}/\text{cm}^2$  [Fig. 3(c)]. Although these polarization values are an order of magnitude smaller than those reported for 2D ferroelectricity,<sup>[43,44]</sup> the breakdown of  $C_3$  symmetry offers an additional route to generate IP electric polarization in doped magnetic monolayer  $\text{VCl}_3$ . In essence, the  $x$ -axis strain leads to a BS-AFM to FM transition through orbital ordering accompanied by an increase in IP electric polarization in electron-doped monolayer  $\text{VCl}_3$ , as shown in Fig. 3(c). In other words, such strain evokes concurrent magnetic and electric polarization changes at the transition.

In addition to uniaxial  $x$ -axis strain, we have also considered uniaxial  $y$ -strains and biaxial epitaxial strains, observing orbital ordering driven transitions among different magnetic orders under strains up to  $\pm 5\%$ . For the uniaxial  $y$ -axis strain [Fig. 4(a)], a BS-AFM to BN-AFM transition is observed for monolayer  $\text{VCl}_3$ . The BS-AFM configuration retains its superior stability from  $-5\%$  to  $1\%$ , and the BN-AFM configuration emerges as the ground state for tensile strains exceeding  $1\%$ . For the biaxial strains, the BS- and BN-AFM configurations appear to be nearly degenerate within a strain range from  $-5\%$  to  $5\%$  [Fig. 4(b)]. At a biaxial tensile strain of  $3\%$ , an orbital-ordering-driven magnetic transition is observed from the BS (BN)-AFM [blue (red)] to the ZZ-AFM configuration (green), resembling the uniaxial  $x$ -axis strain case shown in Fig. 2(a). These results reinforce the observed robustness of orbital-ordering driven changes in magnetism.

In summary, we theoretically investigated the magnetic and electric polarization properties of monolayer  $\text{VCl}_3$  under the influence of uniaxial and biaxial epitaxial strains. The application of epitaxial  $x$ -axis strain distorted the shape of the  $\text{V-Cl}_6$  octahedron, affecting the arrangement in energy levels among two  $e_g^*$  and one  $a_{1g}$  orbitals of the V cation. This modification in orbital ordering precipitated two representative magnetic transitions from the BS-AFM to the ZZ-AFM and subsequently to the FM order under tensile  $x$ -axis strain. Comparable transitions were also observed in the monolayer subjected to biaxial strains. Induced charge doping applied to the bottom layer Cl atoms compromised the structural inversion symmetry of the monolayer, thereby generating an OOP electric polarization. Furthermore, the additional breakdown of  $C_3$

rotational symmetry added an IP component to electric polarization. The magnitude of electric polarization varied across different magnetic orders, establishing a relationship between magnetism and electric polarization in monolayer  $VCl_3$ . Our results suggest that strain-induced rearrangement in orbital ordering offers a novel route to select specific magnetic or electric polarization states in strategically strained open-shell monolayer  $VCl_3$ . This strategy may be applicable to other open-shell 2D magnets. The exploration of the roles of orbital ordering in modulating the magnetic, optical, and electric properties of open-shell 2D magnets remains an open field, necessitating further theoretical and experimental investigations.

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